## Math 1553 Worksheet §6.1-§6.5

1. True/False. Justify your answer.
(1) If $u$ is in subspace $W$, and $u$ is also in $W^{\perp}$, then $u=0$.
(2) If $y$ is in a subspace $W$, the orthogonal projection of $y$ onto $W^{\perp}$ is 0 .
(3) If $x$ is orthogonal to $v$ and $w$, then $x$ is also orthogonal to $v-w$.
2. a) Find the standard matrix $B$ for $\operatorname{proj}_{L}$, where $L=\operatorname{Span}\left\{\left(\begin{array}{c}1 \\ 1 \\ -1\end{array}\right)\right\}$.
b) What are the eigenvalues of $B$ ? Is $B$ is diagonalizable?
3. $y=\left(\begin{array}{l}0 \\ 2 \\ 4\end{array}\right), \quad u_{1}=\left(\begin{array}{l}1 \\ 1 \\ 0\end{array}\right), \quad u_{2}=\left(\begin{array}{c}-1 \\ 1 \\ 0\end{array}\right)$
(1) Determine whether $u_{1}$ and $u_{2}$
(a) are linearly independent
(b) are orthogonal
(c) $\operatorname{span} \mathbf{R}^{3}$
(2) Is $y$ in $W=\operatorname{Span}\left\{u_{1}, u_{2}\right\}$ ?
(3) Compute the vector $w$ that most closely approximates $y$ within $W$.
(4) Construct a vector, $z$, that is in $W^{\perp}$.
(5) Make a rough sketch of $W, y, w$, and $z$.
4. Use least-squares to find the best fit line $y=A x+B$ through the points $(0,0),(1,8)$, $(3,8)$, and $(4,20)$.
