Math 1553 Worksheet §6.1 - §6.5

1. True/False. Justify your answer. (1) If *u* is in subspace *W*, and *u* is also in W^{\perp} , then u = 0.

(2) If y is in a subspace W, the orthogonal projection of y onto W^{\perp} is 0.

(3) If x is orthogonal to v and w, then x is also orthogonal to v - w.

2. a) Find the standard matrix *B* for proj_L , where $L = \operatorname{Span} \left\{ \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix} \right\}$.

b) What are the eigenvalues of *B*? Is *B* is diagonalizable?

3.
$$y = \begin{pmatrix} 0 \\ 2 \\ 4 \end{pmatrix}, \quad u_1 = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}, \quad u_2 = \begin{pmatrix} -1 \\ 1 \\ 0 \end{pmatrix}$$

(1) Determine whether u_1 and u_2
(a) are linearly independent
(b) are orthogonal
(c) span \mathbb{R}^3
(2) Is y in $W = \operatorname{Span}\{u_1, u_2\}$?

- (3) Compute the vector w that most closely approximates y within W.
- (4) Construct a vector, z, that is in W^{\perp} .
- (5) Make a rough sketch of W, y, w, and z.

4. Use least-squares to find the best fit line y = Ax + B through the points (0,0), (1,8), (3,8), and (4,20).