

## MATH 2601 - FoMP - Homework 5

**Instructor** : Prasad Tetali, office: Skiles 132, email: tetali@math.gatech.edu

**Due: Friday, October 19, in class**

**Problem 1.** Suppose that  $G$  is a planar graph on  $n$  vertices and  $m \geq 2$  edges, but with *no 3-cycles*. Then show that  $m \leq 2n - 4$ .

*Hint:* As in the proof done in class, use the Euler characteristic that  $n - m + f = 2$ , for a connected planar graph drawn in the plane with  $f = \#$ faces, and  $n$  and  $m$  being as above.

**Problem 2.** Show that  $K_5$  and  $K_{3,3}$  are nonplanar, using the upper bounds on the number of edges in a planar graph.

**Additionally,** the following problems from Hammack's book:

Chapter 8: 2, 8, 18

Section 11.1: 8, 16

Section 11.2: 4, 6, 10