Math 3012 A1 Test 3 November 19, 2001

Please write legibly, and answers without explanation are not acceptable.

- 1. (6) Find all non-isomorphic simple graphs on 4 vertices.
- 2. (4) Let *G* be the graph given below.
 - a. Find the number of spanning subgraphs in G.
 - b. Find the number of spanning subgraphs of G containing no cycles.

(Sorry, I don't know what the graph sown was. Ask Professor Yu!)

3. (4) Find the chromatic polynomial of the graph described below, and find the number of proper colorings with 5 colors.

(See number 2!)

- 4. (10) Let *G* be the simple graph with degree sequence 6,6,6,6,6,6,7,7,7,7,7.

 Determine the number of edges in *G*. Does *G* contain a Hamiltonian cycle? Is *G* connected? Does *G* have an eulerian circuit? Is *G* planar? Explain your answers.
- 5. (6) Determine whether the following graphs are planar (by finding a plane representation or by finding a subdivision of $K_{3,3}$ or K_5 .)

(See number 2!)