

QUIZ X

Time: 10min

1. Let V be the space spanned by $\mathbf{v}_1 = \cos^2 x$, $\mathbf{v}_2 = \sin^2 x$, and $\mathbf{v}_3 = \cos 2x$.

(a) Show that $S = \{\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3\}$ is not a basis for V .

(b) Find a basis for V .

2. Determine the dimension of and a basis for the solution space of the system:

$$\begin{array}{rccccrcr} x_1 & + & x_2 & - & x_3 & = & 0 \\ -2x_1 & - & x_2 & + & 2x_3 & = & 0 \\ -x_1 & & & + & x_3 & = & 0 \end{array}$$

Each problem is worth 5 pts.