

QUIZ 4

Time: 10min

1. True or false? Justify your answer.

- (a) If none of the \mathbf{R}^3 vectors in the set $S = \{\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3\}$ is a multiple of one of the other vectors, then S is linearly independent.
- (b) If a system of linear equations has two different solutions, then it must have infinitely many solutions.

Each part is worth 5 points.

Bonus (5 points) Let $T: \mathbf{R}^n \rightarrow \mathbf{R}^m$ be a linear transformation. Prove that T is one-to-one if and only if the equation $T(\mathbf{x}) = \mathbf{0}$ has only the trivial solution.