

CHRONOLOGICAL PUBLICATION LIST

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Papers are listed in chronological order of their initial creation. Boldface titles indicate original research results published in refereed research journals, including refereed research-tutorials. Other titles include refereed book chapters and all non-refereed works. Papers which have been reviewed in *Mathematical Reviews* (MR) or *Zentralblatt für Mathematik und ihre Grenzgebiete* (Zbl.) specify the review locations. All papers are available by mail or email upon request, and many papers are available electronically at the address <http://www.math.gatech.edu/~heil>.

1. C. Heil, “A Basis Theory Primer,” manuscript (1987, revised 1997), 93 pages.
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11. C. Heil, *Methods of solving dilation equations*, in: “Probabilistic and Stochastic Methods in Analysis, with Applications” (Il Ciocco, 1991), J. S. Byrnes, et al., eds., NATO Adv. Sci. Inst. Ser. C: Math. Phys. Sci. **372**, Kluwer Acad. Pub., Dordrecht (1992), pp. 15–45. MR 93h:42023. Zbl. 0761.93040.
12. J. Benedetto, C. Heil, and D. Walnut, *Uncertainty principles for time-frequency operators*, in: “Continuous and Discrete Fourier Transforms, Extension Problems and Wiener-Hopf Equations,” Oper. Theory Adv. Appl., **58**, I. Gohberg, ed., Birkhäuser, Basel (1992), pp. 1–25. MR 94a:42041. Zbl. 0790.42017.
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