

MATH1502 A1 and A2, Quiz 2, May 29, Summer 2007

NAME:

Problem 1 (10 points). Evaluate $\int_0^{\infty} x e^{-x} dx$. (Hint: integration by parts).

Same as B.

Problem 2 (10 points). Decide whether $\sum \frac{2+\sin k}{k^2}$ converges.

$$\sum \frac{2 + \sin k}{k^2} \leq \sum \frac{3}{k^2} : \text{conv by } p\text{-series}$$

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I =

Problem 1 (10 points). Evaluate $\int_0^{\infty} x e^{-x} dx$. (Hint: integration by parts).

$$I = \lim_{b \rightarrow \infty} \int_0^b x e^{-x} dx$$

$$u = x \quad dv = e^{-x} dx$$

$$du = dx \quad v = -e^{-x}$$

$$I = \lim_{b \rightarrow \infty} -x e^{-x} \Big|_0^b - \int_0^b -e^{-x} dx$$

$$= \lim_{b \rightarrow \infty} -x e^{-x} - e^{-x} \Big|_0^b$$

$$= \lim_{b \rightarrow \infty} \frac{-b}{e^b} - \frac{1}{e^b} + 0 + e^0$$

$$= 1$$

Problem 2 (10 points). Decide whether $\sum \frac{2 + \cos k}{k^2}$ converges.

$$\sum \frac{2 + \cos k}{k^2} \leq \sum \frac{3}{k^2} : \text{converge by } p\text{-series} \\ (p = 2 \geq 1)$$